

## ECONOMIC GOVERNANCE 2 – SOME FORMAL MODELS

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### Modeling Choices

- [1] Player's strategy choices individual (non-cooperative) or joint (cooperative)?  
Usual: non-cooperative game; ask if Nash eq'm has implicit cooperative outcome.
- [2] How much rationality (individuals' knowledge of rules of game, consistent objective function, perfect calculating ability)?  
Choice here: individuals rational; but Nash equilibrium often suboptimal.
- [3] Equilibrium (of one-shot or repeated game as relevant) versus disequilibrium or evolutionary dynamics.  
Here: focus on equilibrium; add informal discussion of dynamics.
- [4] Nature of games and what is needed to achieve good outcomes:  
Assurance – focal points. Prisoners' dilemma – punishments or rewards.  
Bargaining / battle of sexes – assignment of roles and rights; enforcement
- [5] Good case studies have a lot of rich detail. A lot remains even after someone has modeled a part of it theoretically.

# 1. For-Profit Contract Enforcement

Based on Dixit Lawlessness Ch.4, Econometrica 2003

Key issues in resolution of prisoners' dilemma problems –  
collection and transmission of information; punishment of cheaters

These also a profit-opportunity for someone who can solve them  
(Every economic problem is an economic opportunity.)

Like solving double-coincidence-of-wants problem  
by issuing money and collecting seignorage

Often done by organized crime, in niches where  
government fails, or chooses not to enforce

Gambetta's "generic mafioso" Don Peppe offers both kinds of services

Both sides of the transaction willingly use him

Fees for enforcement larger than for information

Obvious cost-side explanations, but Peppe has territorial monopoly  
and prices above cost, so need demand-side explanation.

Converts one-shot games between anonymous matched pairs  
into pairs of bilateral repeated games of him with the two traders

But cannot offer all-or-nothing deal to whole group,  
so no Coase Theorem optimum either

## Prisoners' dilemma stage game

		Player 2	
		Honest	Cheat
Player 1	Honest	$H, H$	$L, W$
	Cheat	$W, L$	$C, C$

Outside option 0; assume  $W > H > C > 0 > L$   
(If  $C < 0$ , then no play if no enforcement; payoff 0.)

Everyone plays every period but few/no repeat pairs.

Effective discount rate  $r$  includes pure discounting  
as well as the players' survival probabilities

Dixit Econometrica (2003) has model with asymmetric payoffs, types.

## Intermediary

Contestable profit-motivated monopolist, keeps track of cheating,  
sells information or enforcement services

Intermediary's honesty not guaranteed or enforceable  
need conditions to rule out deviation

## Information intermediary (Info)

For appropriate fees, he can:

Reveal – to customer his private info about previous actions of partner

Double-cross – take fee from customer on one side, and another

from the other side in return for letting him cheat the customer

When someone cheats a non-customer, Info keeps no record of this, thereby automatically avoids “free-riding” on his existence.

## All-customer, honest equilibrium

Conditions (bounds on Info’s fee) to rule out deviations:

Customer’s cheating:  $F \leq (H - C) - r(W - H)$

Info’s double-crossing:  $F \geq r(W - H)$

Each side must have enough share of rent / surplus

If monopolist Info sets fee, will set it at upper bound

If group hires Info, fee at lower bound. Or intermediate – Nash bargaining.

Conditions harder to satisfy if  $r$  larger, which happens if

individuals more impatient or have higher mortality probabilities

So enforcement harder if “cutthroat competition” among rival mafias

## Enforcement intermediary (Enfo)

Enfo can punish any trader who cheats his customer

Assume punishment sufficiently severe to be effective deterrent

So not used, but Enfo needs reputation for credible threat

Condition to rule out double-crossing similar to Info's

In all-customer equilibrium, Enfo's fee must satisfy  $F \leq H$

This exceeds Info's fee (fits Gambetta's evidence). Demand-side reasons:

[1] Enfo does not have to share any rent

[2] Enfo's customers have worse outside opportunities if  $C > 0$

Deviant non-customers cannot get  $C$ ; must opt out of game

But Enfo mode not dominant: entry cost may be higher than for Info

## Social optimum comparisons

Social gain from honesty vs. cheating =  $H - C$

Info's fee =  $(H - C) - r(W - H) < \text{social gain}$

Enfo's fee =  $H > \text{social gain}$  when  $C > 0$  (else equal)

But individuals trapped, cannot switch equilibrium

Related to Bandiera's idea of negative externality.

## **Evaluation – Achievements**

Explains some basic facts:

- Both sides use and pay for intermediary services

- Fee for enforcement higher than that for information service

Generates some new results that can be tested:

- Enforcement mode more likely to result in bad equilibrium

## **Shortcomings and Research Opportunities**

Touches on only small fraction of rich case / ethnographic detail

Endogenize occupation choice between trading and protecting  
including issue of vertical integration by mafia

Mafia may offer protection only to selected subset of traders  
and use deliberate “regulated injection of distrust”

Should examine [1] Links among multiple functions of intermediation

- improving search and matching, connection between different networks, ...

- [2] Internal structure of mafia; reputation-building, information flow

## 2. Relational and Formal Contracts

Example of private ordering “in the shadow of the law”

Dixit Lawlessness Ch. 2, Baker, Gibbons, and Murphy QJE 1994

General idea: Private ordering can use better inside information, but must be self-enforcing, based on repeated relationship, reputation

Less precise but verifiable public information exists

Formal contract enforceable in court can be based on this

Revert to this if cheating in relational system

Incentive compatibility (IC) constraint for relational contract

$$V(\text{cheat}) + \frac{V(\text{formal contract})}{r} \leq V(\text{honest}) + \frac{V(\text{honest})}{r}$$

Better to use relational contract if  $V(\text{formal contract}) < V(\text{honest})$

But lock-in to wrong equilibrium remains possible.

Partial improvement in quality of formal system tightens IC constraint; this worsens performance of relational contract

This analysis is one aspect of the Coase-Williamson question:

“What determines boundary between firm and market?”

More generally, for any repeated game with outside option

### 3. Limits of Self-Governance

Case studies of self-enforcing trade or cooperation in communities emphasize importance of interactions and information transmission  
Greif's contrast between Maghribi and Genoese traders and Li's findings in E. Asia, Ostrom's cases show that increase in size of groups leads to decay of these  
Construct model to understand this process and its implications

#### The model

From Dixit Lawlessness Ch.3, J. Pol. Ec. 2003  
Continuum of traders along circle, circumference  $2L$   
Two periods, random IID pairings in each period  
Distance from current partner  $x$

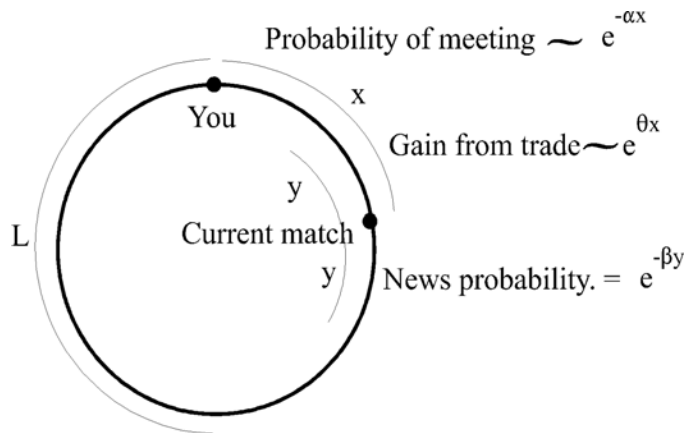
Localization of meetings: Probability of match at  $x$  is  $\propto e^{-\alpha x}$

Localization of information: Probability of news spreading  $= e^{-\beta y}$

Desirability of expansion: Size of potential gain is  $\propto e^{\theta x}$



Figure illustrates the concepts



Random matches in first period play prisoner's dilemma game

If cheat, the news may spread, leading to worse payoff

in game with random second-period partner

Condition for self-enforcing honesty : immediate gain

should be less than expected future loss, which is

complicated expression integrating along circle

Extra payoff from sustaining first-period honesty up to  $X$  is

$$V(X, L) = \frac{\alpha}{\alpha - \theta} \frac{1 - e^{-(\alpha - \theta)X}}{1 - e^{-\alpha L}}$$

In particular, graph of  $V(L, L)$



Need  $\alpha > \theta > 0$

## General results

[1]  $X = L$  possible for  $0 \leq L \leq L^*$

[2] As  $L \uparrow$  beyond  $L^*$ , maximal  $X \downarrow$  unless  $\beta$  is small relative to  $\theta$

Intuition seen from figure:



Circle on left of critical size  $L^*$ . O when meeting P  
is indifferent between honesty and cheating

Circle on right is somewhat larger;

$OP_1 = OP_2 = L^*$ , with added people between

If O cheats  $P_1$ ,  $\text{Prob}\{P_2 \text{ finds out}\}$  now  $< 1$ ; was  $= 1$ .

This lowers cost of cheating. The larger is  $\beta$ , the bigger this effect

If O cheats  $P_1$ , he risks his period-2 meetings between  $P_1$  and  $P_2$

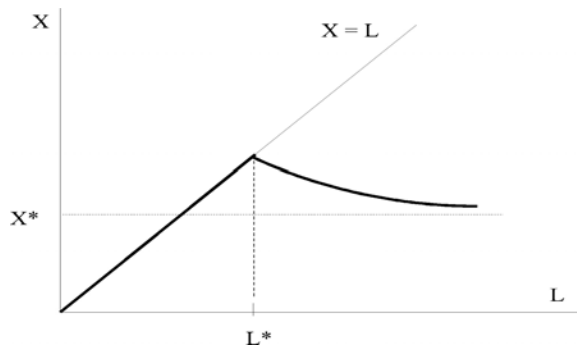
This raises cost of cheating. The larger is  $\theta$ , the bigger this effect

Numerical calculations show that for plausible values, former effect bigger

[3] As  $L \uparrow \infty$ , maximum possible  $X \downarrow X^*$ ;

if  $\beta$  is large,  $X = 0$  for finite  $L$

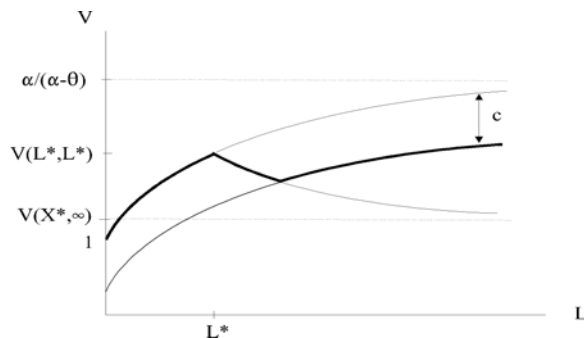
Typical picture:



[4] Allow external governance at cost  $c$  per unit arc length of circle,  
 Benefit of self-governance as a function of  $L$  is  $V(L, L)$  for  $0 \leq L \leq L^*$ ,  
 then decreases, asymptotes to  $V(X^*, \infty)$

Benefit of external governance =  $V(L, L) - c$  for all  $L$ .

Take the upper envelope of these:



For small  $L$ , self-governance is optimal.

For large  $L$ , external governance may become optimal if  $c$  is small enough

But payoff may not rise back to  $V(L^*, L^*)$  – “anti-globalization theorem” :-)

Middle range of  $L$  too large for self-governance and too small for external

## Evaluation – Achievements

Explains some basic facts:

- Explains limit on size of multilaterally self-governing groups in terms of parameters of information and communication technology

Generates some new results that can be tested:

- Intermediate size worse for governance than either extreme

## Shortcomings and Research Opportunities

Uses comparative statics methodology instead of proper dynamics of transition, with expectation, collective action, and lock-in problems

Other models of evolutionary dynamics exist, but compensate by simplifying the underlying transaction game, communication etc.

Should link multiple functions of trading groups:

- improve search and matching, combine with social activities, ...

Should explore more formally how trade can occur between

- Greif's collectivist and individualist (Li's relation and rule based) societies: Does one have an advantage? Role for intermediaries?

Alternative approaches: Disjoint groups; discrete networks

## Network-theory modeling

Individuals are at discrete nodes; may be linked to other nodes

Random graph theory of Erdős and Renyi:

Probability that any two nodes are linked is  $p$

Then in network with  $n$  nodes, probability that

two given individuals have a common acquaintance is

$$A(n) = 1 - \left( 1 - p^2 \right)^{n-2}$$

As  $n \rightarrow \infty$ ,  $A(n) \rightarrow 1$  “large world” theorem!

Now suppose  $p = p(n) \propto n^{-\theta}$ , consider large  $n$

If  $\theta > 1/2$ , then  $A(n) \rightarrow 0$

If  $\theta = 1/2$ , then  $A(n) \rightarrow \text{limit} > 0$  and  $< 1$

If  $\theta < 1/2$ , then  $A(n) \rightarrow 1$

Can do similar calculations for longer links etc.

Recent work on non-random graphs leading to power laws etc. See

A-L. Barabasi, *Linked: The New Science of Networks*, 2002

D. Watts, “The new science of networks,” *Ann. Rev. Soc.* 2004  
and the references cited there.

Some measures/properties of non-randomness:

[1] Local clustering – a measure of local link density

What fraction of my links have direct links with each other?

[2] Average shortest path length between two nodes

Over broad range of parameter spanning extremes of order and randomness, high clustering compatible with short average paths (small world networks of the “six degrees of separation” fame).

[3] Probability of link  $p$  varies  $\propto r^{-\gamma}$ ; parameter measures localness

[4] Searchability – can navigate best path to distant node using only local information at each step

This can require coincidence of  $\gamma$  and network dimension

[5] Power laws: In many networks, Prob(given node has  $k$  links) is  $\propto k^{-\alpha}$ .

This yields a few well-connected nodes and many with few links

Raja Kali, “Social embeddedness and economic governance,”

<http://www.idei.fr/doc/conf/jjl/papers/105kali.pdf>

uses a small-world network for model similar to the circle above.

Potential use for better models of matching and information flow.