The interdependence of domestic and international success: the case of the UEFA Champions League

Juan Moreno-Ternero and Shlomo Weber

Universidad Pablo de Olavide, New Economic School

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- In 1955, the so-called European Champion Clubs' Cup was launched.
- It was a yearly competition played by the national league champions of the strongest UEFA national associations.
- The competition took on its current name (the UEFA Champions League) in 1992, adding a group stage to the competition and allowing multiple entrants from certain countries.
- It is one of the most prestigious tournaments in the world and the most prestigious club competition in European football.

- In its present format, the UEFA Champions League begins with four knockout qualifying rounds and a play-off round.
- The surviving teams enter the group stage, joining teams qualified in advance.
- Overall, 32 teams are drawn into eight groups of four teams and play each other in a double round-robin system.
- The eight group winners and eight runners-up proceed to the knockout phase that culminates with the final match.
- The eight third-place holders join the UEFA Europa League.
- The eight forth-place holders leave both Champions and Europa League.



- Real Madrid is the most successful club in the competition's history, having won the tournament 13 times
- Spanish clubs have accumulated the highest number of victories (18), followed by England and Italy (12).
- The last 10 Champions League competitions witnessed a very strong domination of Spanish clubs:
 - Real Madrid won 4 competitions and Barcelona 3.
 - Atletico de Madrid was a runner-up in 2 editions.
 - The UEFA Europa League, also witnessed a similar domination of Spanish clubs who won it 6 times in the last decade, Atletico Madrid and Sevilla - 3 times each.
 - What could possibly be the reasons for such a streak?



- One hypothesis is that Spain enjoyed during the last decade two of the most dominating players in history (Lionel Messi and Cristiano Ronaldo) who received the so-called Ballon d'Or (the most prestigious annual football award, awarded since 1956) five times each for the period from 2008 to 2017.
- Actually, for those 10 years there was only one runner-up not named Ronaldo or Messi (Andres Inesta in 2010).
- Here, we consider a different hypothesis referring to the interdependence of domestic and international competitions.

- During the last decade, the Spanish domestic competition was indeed characterized by the rivalry between the two powerhouses (Barcelona and Real Madrid), each having one of those two dominant players. But this involved a great amount of effort (and stress) to win domestically (especially during the Guardiola-Mourinho era).
- In general, none of this two teams won easily the domestic competition as opposed, for instance, to Germany and Italy, where Bayern Munich and Juventus exhibited an overwhelmingly domination in the last years.
- On the other hand, with the occasional exception of Atletico de Madrid (an important actor in the UEFA CL too), they faced little competition from other teams in La Liga, as opposed, for instance, to England, which witnessed 4 different champions in the last 7 seasons of the EPL.



A simple model

Let N be the set of domestic (national) competitions. For each competition $i \in N$, we denote by

- λ_i the country coefficient associated to it (a strength of the domestic league determined by UEFA)
- b_i competitive balance associated to it
- p_i the probability that a team from competition i wins the international tournament.
- the competitive balance can be represented either by HHI, the ratio of the Hirschman-Herfindahl index to that of the perfectly balanced league
- the concentration ratio the share of points of the top 5 teams as compared to that share of the perfectly balanced league
- the standard deviation of the league points.



A simple model

$$p_i = \frac{f_i(G_i)}{\sum_{j=1}^n f_j(G_j)},$$

We assume:

- $f_i \leq f_j$ for each pair $i, j \in N$, such that $\lambda_i \leq \lambda_j$.
- $G_i = G_i(b_i)$, for each $i \in N$

We then suggest:

$$G_i(b_i) = (M - b_i)b_i^{\alpha_i},$$

where M denotes the upper bound of b_i , and $\alpha > 0$ denotes the rate of substitution of competitive balance and performance dispersion for the determination of effort.

Note that
$$\frac{\alpha_i}{1+\alpha_i}M = \arg\max_{[0,M]} G_i(b_i)$$
.



A simple model

Consequently,

$$p_i = \frac{\lambda_i (M - b_i) b_i^{\alpha_i}}{\sum_{j=1}^n \lambda_j (M - b_j) b_j^{\alpha_j}},$$

which could be simplified assuming $\alpha_i = \alpha$, for each $i \in N$.

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				RANC	O PERMAI						
1,3158	1,68421	1,5	1,41176	1,526316	1,394737	1,5	.,0_00	1,36842	1,10526	1,36842	1,5
0.8421	0.78947	0.60526	0,85294	0.684211	CHAMPION 0.473684	0.55263		0.76316	0.39474	0.71053	1,0588
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18,227	19,1709	20,551	13,988	20,62567	19,85102 C\	20,7973	13,9406	18,1032	15,4384	17,247	15,503
0.3459	0.36832	0.38886	0.30154	0.392496	0.375966	0.3924	0.29731	0.34548	0.2989	0.33009	0.3249
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0.4046	0.40007	0.04440	0.45700	0.040000	GIN		0.45440	0.47040	0.40007	0.47044	0.4040
0,1845	0,19207	0,21112	0,15788	0,216603 R	0,199716 ANGO CAM			0,17319	0,16297	0,17641	0,1646
0,5263	0,65789	0,60526	0,85294	0,552632	0,447368			0,71053	0,39474	0,63158	0,9706
	,		,		CAMP+SUE		,	,			
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0,2330	0,24784	0,24002	0,24192	0,246333	0,243371 IQR-N		0,25237	0,2000	0,21491	0,24211	0,2631
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11,25	11,65	12,45	7,5	12,8	12,1		8	10,55	9,25	10,45	8,3333
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0,3624	4 0,38713	0,38505	0,30778	0,38059	0,386364	0,38302	0,32583	0,37691	0,34269	0,36746	0,3271
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0,6233	0,63401	0,65847	0,61317	0,658421	0,639205 HF		0,60545	0,61832	0,61955	0,62392	0,6147
0.0557	0.05644	0,05718	0,06033	0.057318	0,056714		0,06019	0.05567	0,05424	0.05518	0,0611
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5			43		50		56 44
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4			40		45		41
4			40		42		39
3		46 43	37 36		40 38		14 14 36
3			35		38		30
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	0 30	19	SU	MA	3((5)
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443,53684	2 267,292105	259,081579			371,463158	378,26315	301,555556
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0,4473684	4 0,44736842	0,60526316	•	0,52631579 BC-NORM	0,1842105	0,9736842	0,85294118
0,1781609	2 0,15854823	0,15498519			0,16007533	0,1780952	0,18852459
			CAMP+SUE	C+3-NORM			
0,2528735	6 0,23018147	0,2230997	0,25598086	,	0,23728814	<mark>4</mark> 0,2523809	0,26346604
1.2	5 1,15	0,85	-	NORM	1,5	0,9	9 <mark>5</mark> 1,33333333
1,2	1,10	0,00		NORM	1,00	0,0	1,0000000
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52,	52,35	50,65	<u> </u>	52,7	53,1	52	,5 47,4444444
0.3994252	0.35816619	0,34846989		ORM 0.37666034	0.37947269	0,3714285	0,33489461
0,000-202	0,00010013	0,01010000		NORM	0,01011200	- 0,01 1720C	0,00 100 101
0,653256	7 0,62559694	0,62092794	0,60406699	0,62713472	0,65065913	0,6	0,6440281
0.6	0.0546335	0.0545050		HI	0.0506	0.050511	0.000=10=
0,0577318	3 0,05463283	0,05479702		0,05571978 IORM	0,05625778	0,0565188	0,06258467
0.0081387	0.00487666	0,00504949			0.00658714	4 0,0068619	0,00744259
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HICB

HICB							
111,363956	112,887464	114,364837	108,587328				
HICB ranks							
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	HICB-av	verage					
112,848236	111,316935	112,39509	109,527517				
HICB-rank-average							
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	C510	СВ					
144,971537	154,851105	154,020814	134,51497				
	C5ICB	ranks					
2	3	4	1				
	C5ICB-a	verage					
151,681023	148,305718		139,529596				
C5ICB-rank-average							
3	2,8	2,8	1,4				
	SDI	_P					
18,2269321	19,1709072	20,5510276	13,9879734				
SDLP ranks							
2	3	4	1				
SDLP-average							
19,2607207	18,0165598	18,8280677	14,8767564				
SDLP-rank-average							
3	2,4	3,4	1,2				