



**Growth**

# Modern economic growth

- Economic growth is a relatively recent phenomenon
- Maddison:
  - World income per capita same in 500 and 1500 AD
  - In 1500-1820 cumulative growth of 15% (0.04% p.a.)
  - Since then growth at 1.2% a year (doubles every 58 years)

# Growth in this course

- Aggregate growth models

Harrod-Domar

Solow = Harrod-Domar +  
endogenous capital-output ratio

Ramsey = Solow +  
endogenous savings

Endogenous growth = Ramsey +  
endogenous human capital / R&D

- Cross-country evidence
- Micro evidence
- New growth paradigm: disaggregated growth model

# Harrod-Domar

GDP is proportional to physical capital  $Y=AK$   
(neither labor nor human capital matter,  
motivated by Great Depression)

Capital accumulation:  $\Delta K = -\delta K + I$   
( $\delta$  - depreciation rate)

Hence growth is a linear function of  
investment

$$\Delta Y/Y = \Delta K/K = -\delta + I/K = -\delta + AI/Y$$

Investment immediately brings growth

# Numerical example

- Productivity of capital  $A = Y/K = 0.25$  p.a.
- Depreciation  $0.05$  p.a.
- Want to achieve  $6\%$  p.a. growth
- Hence  $0.06 = -0.05 + 0.25 * I/Y$
- Targeted investment rate  
 $I/Y = (0.06 + 0.05) / 0.25 = 0.44$
- What if savings are just  $14\%$  GDP? Then  
'Financing gap'  $= S/Y - I/Y = -30\%$  GDP

# Implications

- Raise investment whatever it takes
- If  $\text{savings} < \text{targeted investment rate}$ , then bridge the financing gap
- Hence: Aid for investment
- BUT: capital flight and misplaced investment
  - Aid is channeled back through offshore

# Soviet industrialization

- Implementation of Harrod-Domar
  - Domar refers to Soviet 1920s economists
- Industrialization within three ‘five-year plans’
  - Impressed many development economists and developing countries
- ‘Perspiration not inspiration’
  - High investment
    - At the expense of consumption
  - Increase in industrial labor force
    - At the expense of agriculture
  - Low (if positive) wages

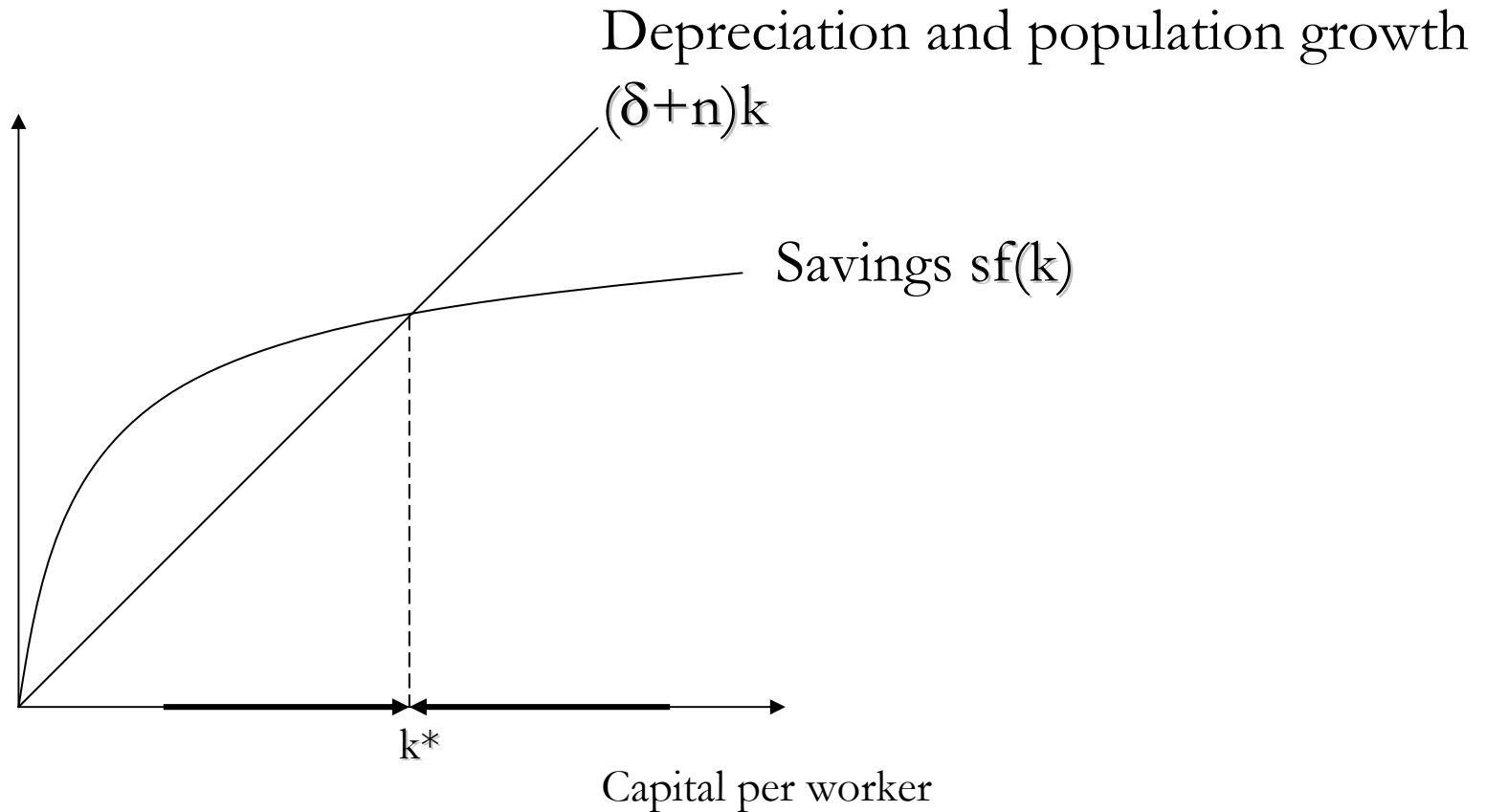
# Solow model

- Substitution between capital and labor
  - Production function  $Y=F(K,L)$ 
    - Constant returns to scale:  $Y=LF(K/L,1)$  or  $y=f(k)$
    - Diminishing returns to each factor:  $f'>0, f'' <0$
  - Harrod-Domar is a particular case with  $Y=AK$ , or  $Y=\min\{AK,BL\}$
  - More general case: substitution, e.g. Cobb-Douglas  $Y=K^\alpha L^{1-\alpha}$
- Labor grows at an exogenous rate  $n$
- Savings rate  $s=S/Y$  is fixed



# Steady state

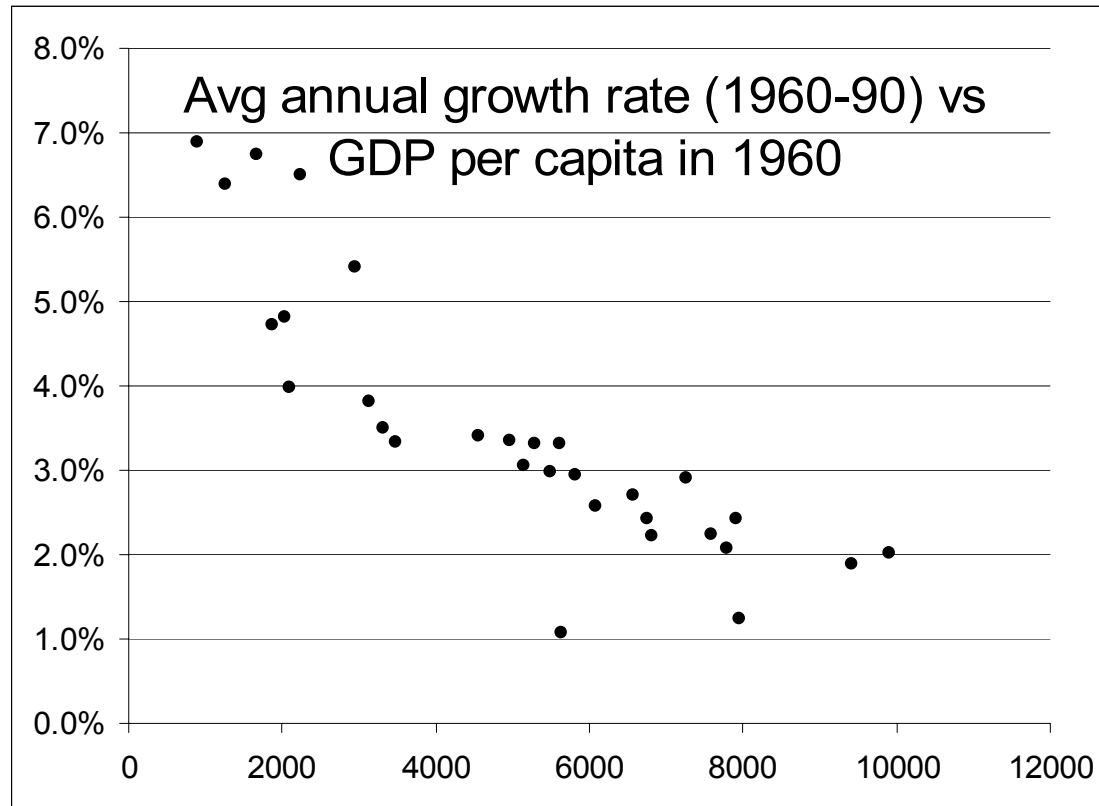
$$dk/dt = sf(k) - (\delta + n)k$$



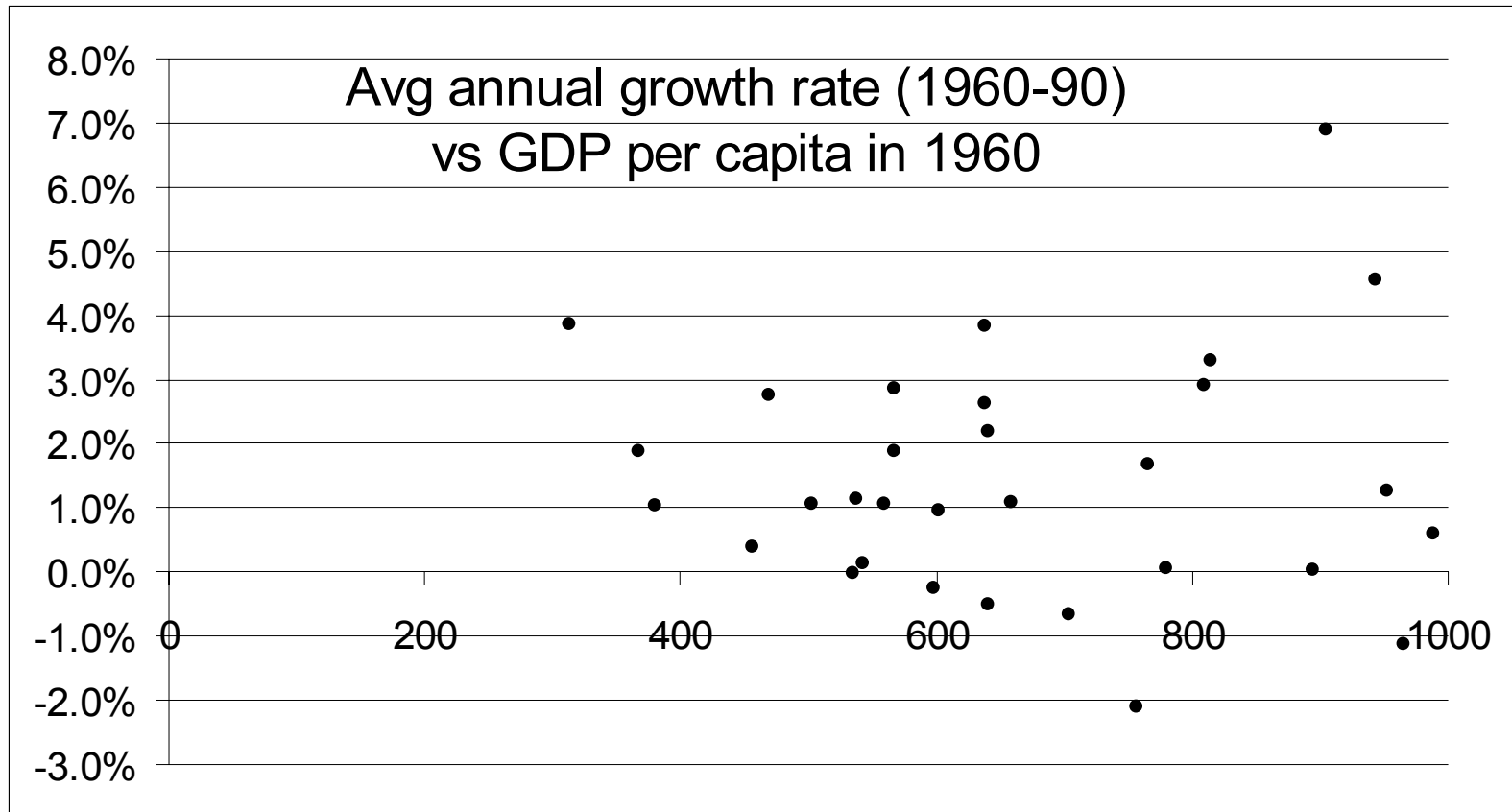
# Solow: Implications

- Long-term: no per capita growth
  - Need models with technological progress to explain growth
  - Savings and population growth only affect
- Short-term: transition path, convergence to the same per capita capital  $k^*$  and per capita income  $f(k^*)$ 
  - All countries have access to frontier technology
  - Backward countries grow faster
  - The lower initial income, the higher the growth rate

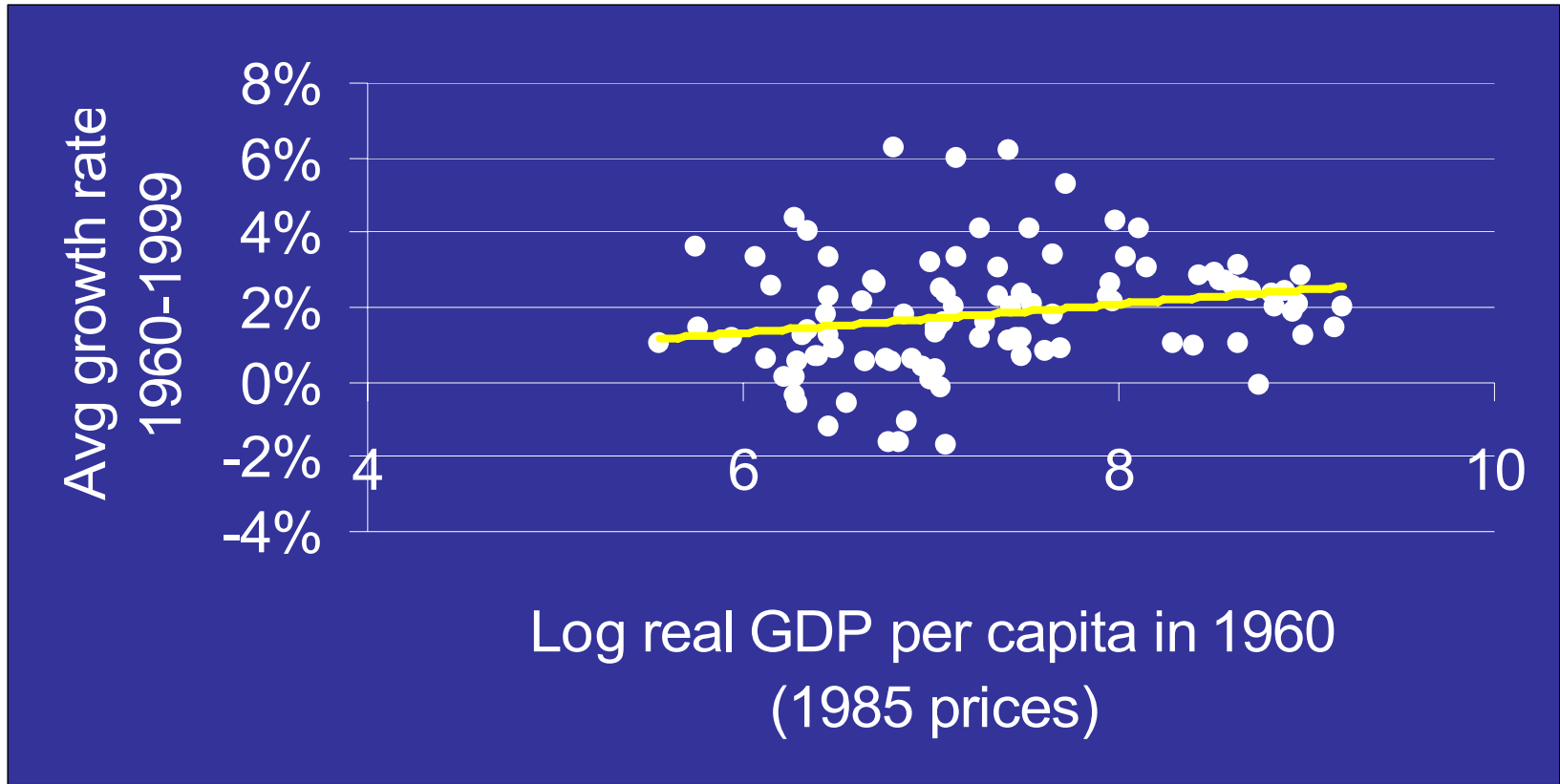
# Evidence (rich countries) ...



# But not for the poor



# Whole sample, 1960-1999

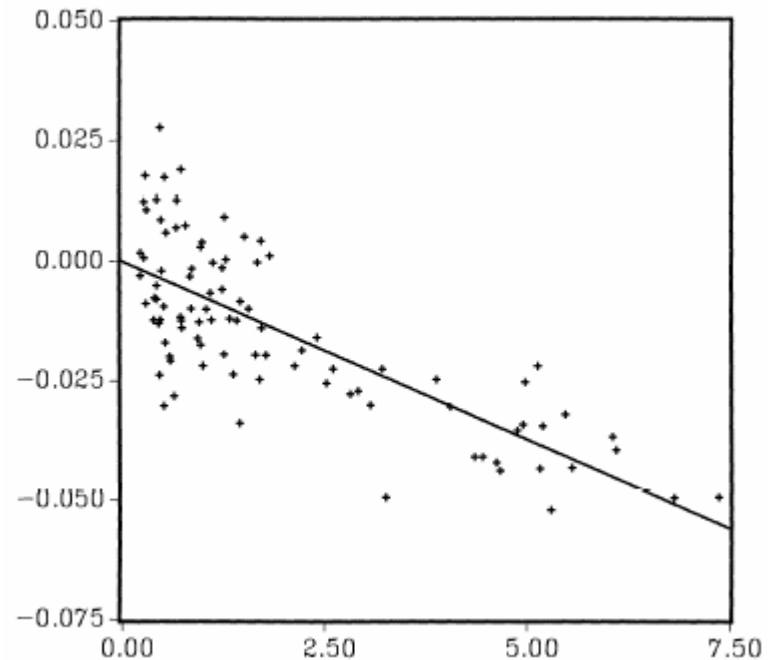
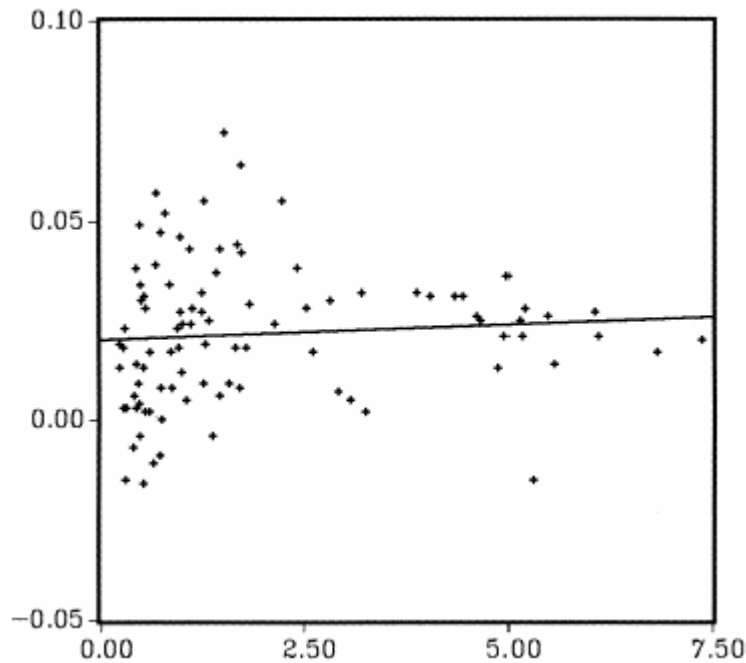


# No absolute convergence

- Neither in the postwar period
- Nor in modern growth era (since 1820, Maddison)
- So all countries grow at the same rate? (could use Harrod-Domar?)
  - Need careful empirical analysis
  - There is *conditional* convergence
    - Countries differ in  $s$  and  $n$
    - Hence may converge to different steady states

# Conditional convergence

- Barro (1991): growth rate as a function of initial conditions (pairwise, left, and controlling for other factors, right)



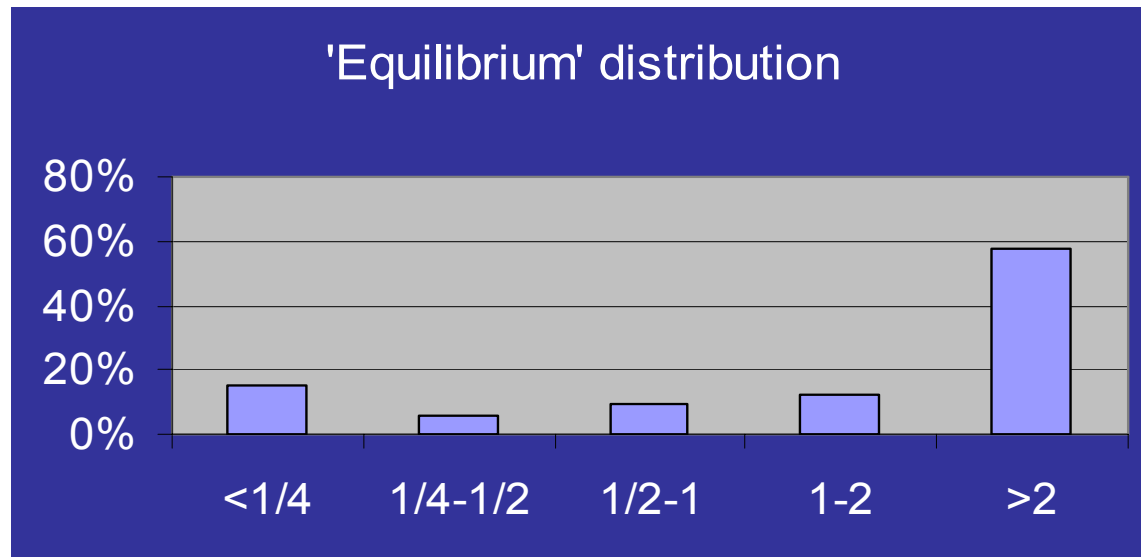
# Mobility matrix (Quah, 1993)

1984 1962	$<1/4$	$1/4-1/2$	$1/2-1$	1-2	$>2$
$<1/4$	0.76	0.12	0.12	0	0
$1/4-1/2$	0.52	0.31	0.10	0.07	0
$1/2-1$	0.09	0.20	0.46	0.26	0
1-2	0	0	0.24	0.53	0.24
$>2$	0	0	0	0.05	0.95



# Implications

- Substantial mobility (both upward and downward) especially in middle-income range
- No convergence: converges to 'bimodal' distribution
  - Word of caution (recent results): standard errors are too large to make any prediction



# 'Convergence clubs'

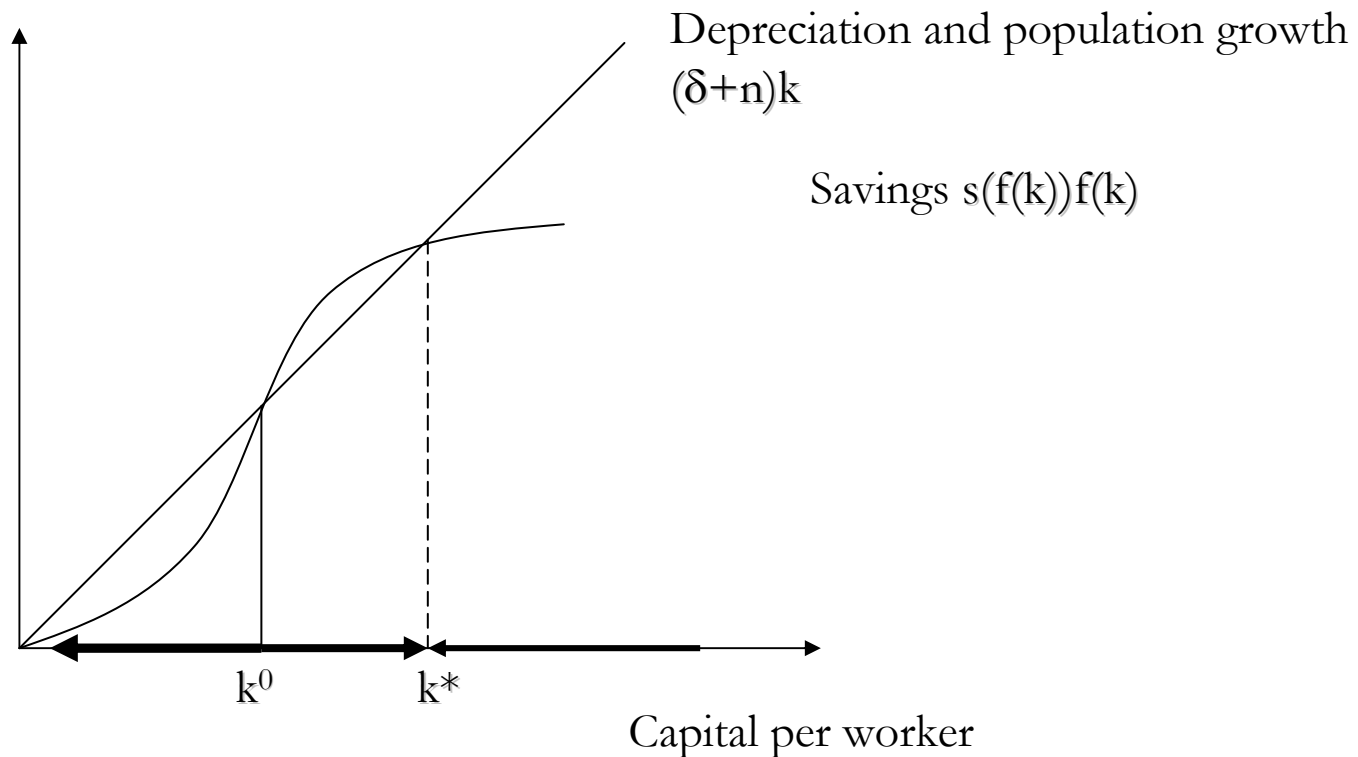
- Several clusters of countries converging to different steady states
  - Some middle income countries 'converge downward'
- Can be explained with underdevelopment traps / multiple equilibria

# Underdevelopment traps in Solow model

- Modified Solow model
  - Subsistence constraint:
    - Savings rate lower at low incomes
  - Population growth
    - Population growth higher at low incomes

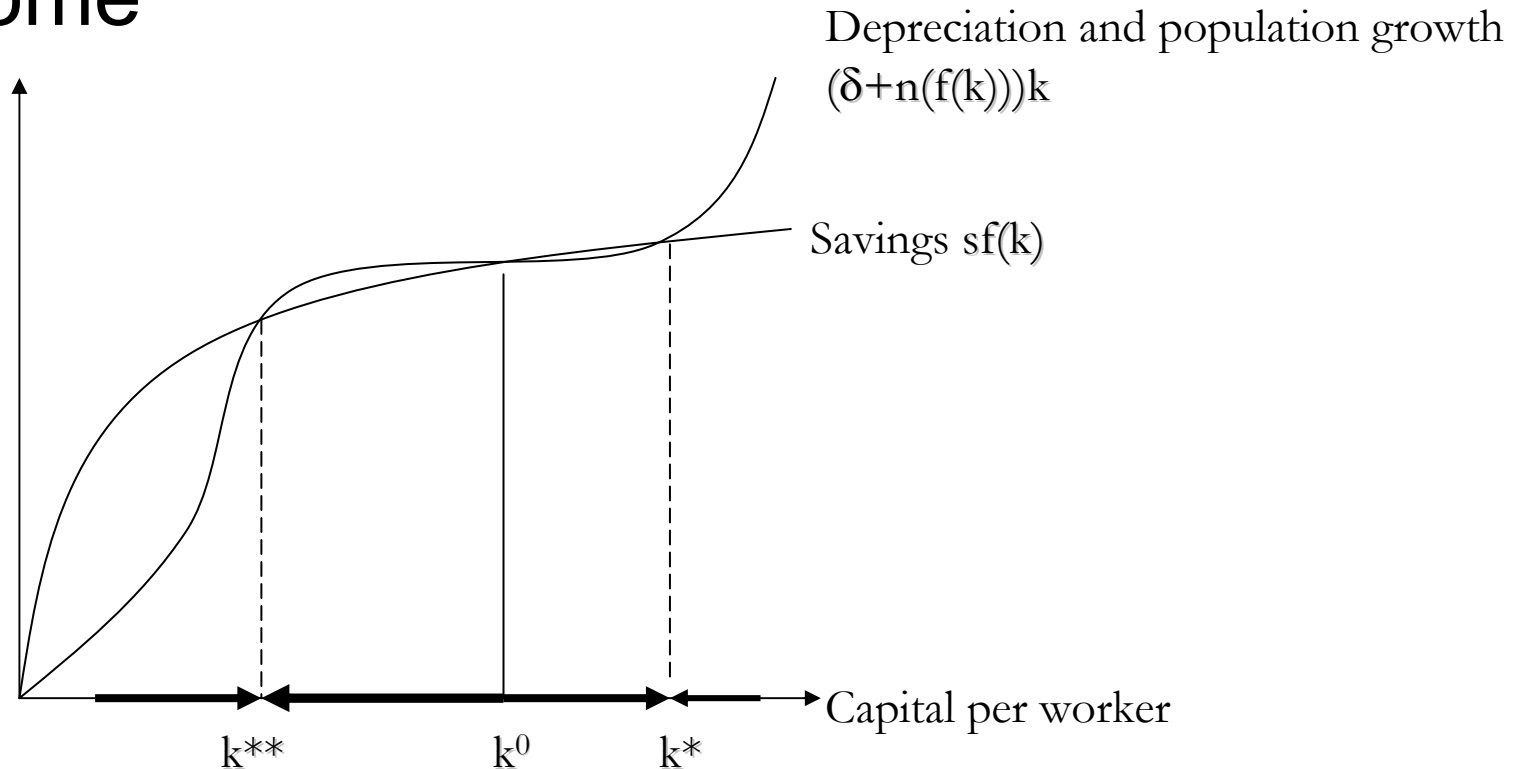
# Subsistence constraint

$s(y)=s(f(k))$  increasing function of income



# Endogenous population

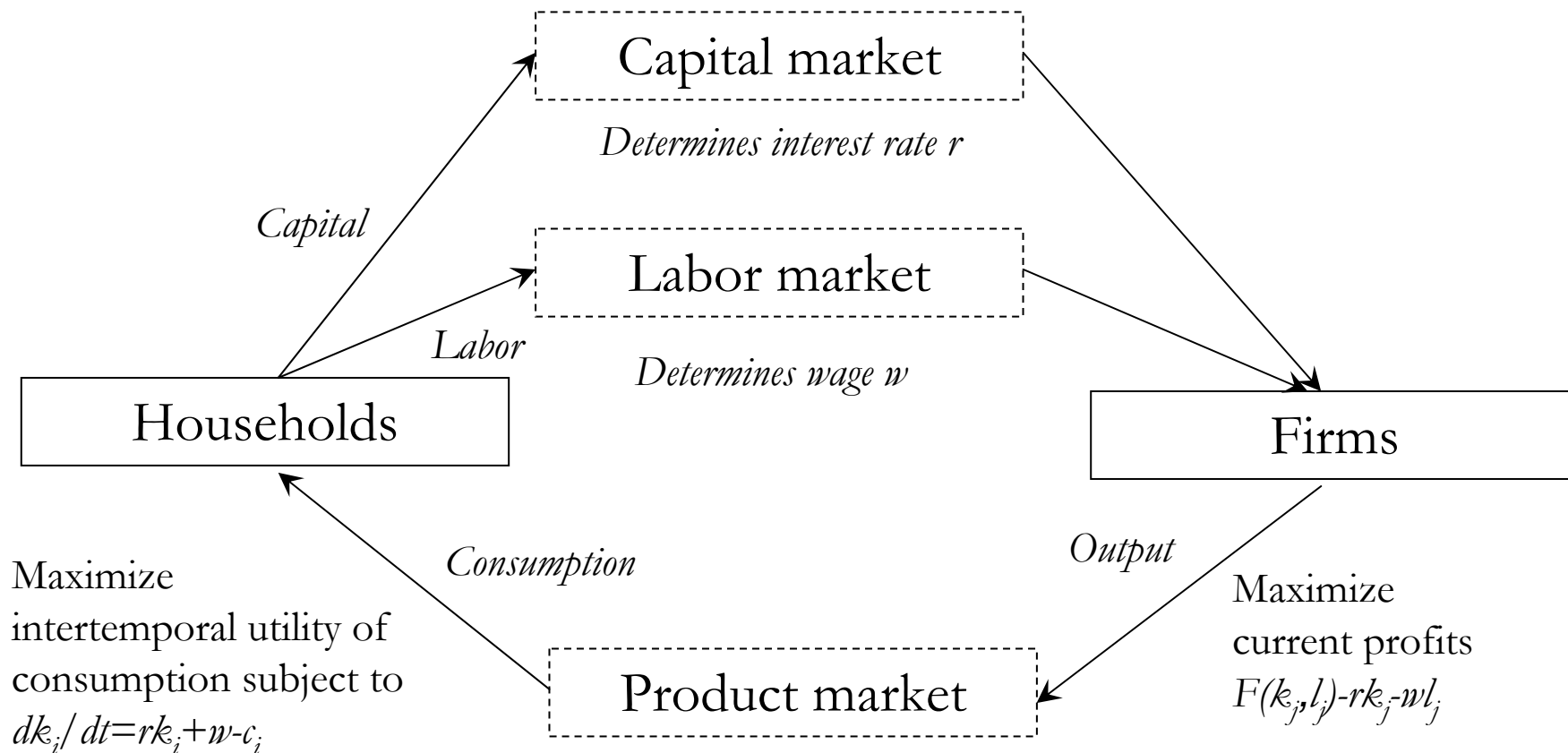
$n(y)=s(f(k))$  increases and then falls with income



# Ramsey model

- General equilibrium model with infinitely lived consumers
- Consumers maximize intertemporal utility subject to budget constraint (wages+capital income=consumption+savings)
  - endogenous savings rate
- Firms maximize profits
- Same results for a closed economy as Solow:
  - Steady state savings rate  $s=(n+\delta)/(n+\delta+\rho)$   
where  $\rho$  is representative consumer's discount rate

# Ramsey: closed economy

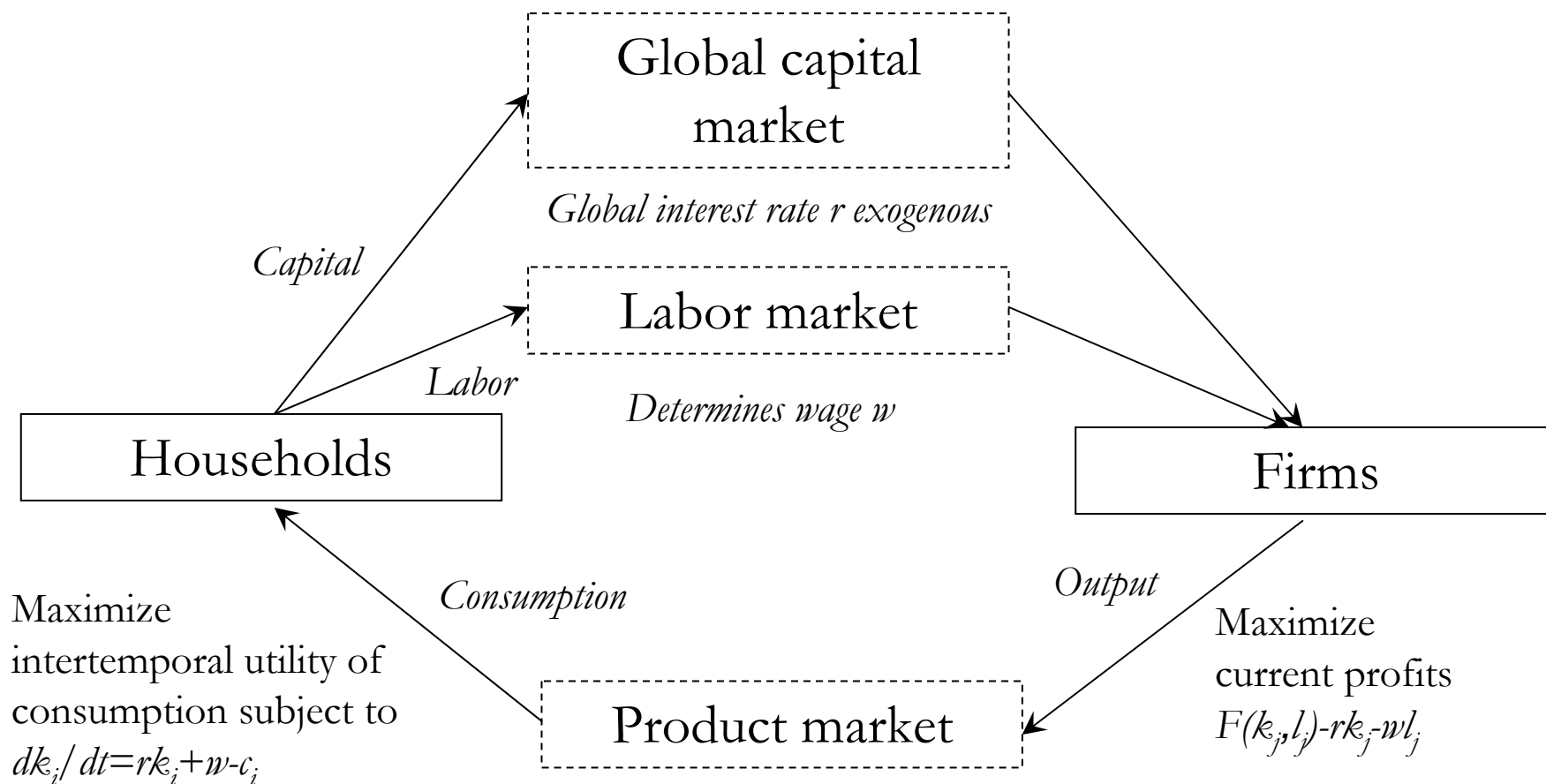


# Ramsey: open economy

- Assumptions:
  - Mobile capital
    - Interest rate should be the same in all economies
  - Immobile labor
    - Countries may differ in terms of wage, capital/worker, income/worker
- Equilibrium
  - Marginal productivity of capital should be higher in poor countries
  - Capital should move from rich to poor countries
- Evidence:
  - US is the largest recipient of FDI
  - OECD receive >90% FDI



# Ramsey: open economy



# Exogenous technical progress:

- To explain growth, add exogenous technical progress
  - $Y=F(K,HL)$
  - Human capital  $H$  grows at an exogenous rate  $\gamma$
- Same, except replacing labor  $L$  with ‘effective labor’  $HL$ 
  - Steady state:
    - Capital per unit of effective labor  $K/(HL)=k^*$  constant
      - Higher  $H \Rightarrow$  Higher capital per worker  $K/L=Hk^*$
    - No growth of output per unit of effective labor,
      - Hence growth per capita at  $\gamma$  per cent p.a.

# Growth accounting and Solow residual

$$Y = A K^\alpha L^{1-\alpha}$$

[ $\alpha$  is estimated using national accounts, share of capital and labor income in GDP,  
L – labor force rather than population]

Hence

$$\Delta Y/Y = \Delta A/A + \alpha \Delta K/K + (1-\alpha) \Delta L/L$$

A – is Total Factor Productivity (TFP)

$\Delta A/A$  – is growth in TFP

(TFP *level* does not matter)

In per capita terms

$$\Delta y/y = \Delta A/A + \alpha \Delta k/k$$

# Growth accounting, numerical example

Capital's share in GDP is 0.3

Capital per worker grows at 10% p.a.

GDP grows at 5% p.a.

Hence TFP grows at  $5 - 0.3 * 10 = 2\%$  p.a.

- Can also adjust for human capital etc.

# Growth accounting and East Asian Miracle

- Korea, Taiwan, Singapore, and Hong Kong have been growing at astronomic rates since 1960
- Worldbank (1993): 'East Asian Miracle', 'productivity-based catching-up'
- Young, Krugman:
  - Mostly based on factor accumulation
    - Education: from 35 to 88%
    - Labor force participation rates: from 27 to 36%
    - Savings rate higher than in other developing economies by 10-20% GDP
  - Growth accounting gives <3% TFP growth
    - Not higher than in other economies

# Factor accumulation is endogenous to technological progress

- Productivity increases incentives to accumulate
  - Human capital
  - Physical capital
- Klenow, Rodriquez-Clare:
  - If take into account the response of capital to TFP growth then TFP growth accounts for a substantial share of East Asian Miracle

# Exogenous technical progress: implications

- Increase in productivity (e.g. education)  $\Rightarrow$  growth of GDP per capita
- Worldbank and others have achieved a dramatic improvement in education in recent 40 years
- No market for human capital  $\Rightarrow$  low quality, inefficient matching, and braindrain
- In most developing countries, modern technologies are accessible, but no incentives to use them

# Education and GDP growth, 1965-85 [Easterly, 2001]

	Education growth, % p.a.	Growth of GDP per capita, % p.a.
Botswana	6	9
Lesotho	2	5
Senegal	7	-1
Madagascar	5	-1
Ghana	4	-1
Subsaharan Africa	4	0.5
East Asia	3	4



# Endogenous growth and increasing returns

- Technology is non-excludable (leakages)
  - Constant returns at individual level but increasing returns at the economywide level
- Technology is non-rival
  - Once the technology is invented, marginal cost of dissemination is low
- Critical mass effect in R&D
- ‘Standing on shoulders of giants’: sequential innovation, threshold externalities
- Evidence: Kremer (1993)
  - Non-rivalry of technology, hence higher population  $\Rightarrow$  higher growth
  - Consistent with longest-term data
- Geographical concentration of innovative activity
- Increasing returns  $\Rightarrow$  Multiple equilibria

# Endogenous growth theory

- Rational choice of R&D
- Technological progress is endogenous
- Schumpeterian growth:
  - Creative destruction
- Intellectual property rights and licensing:
  - Incentives to innovate vs dissemination of knowledge
- Imitation vs. innovation:
  - Different policies in early and later convergence

# Increasing returns and Big Push

## Big Push and market size externality

- Rosenstein-Rodan (1944) formalized by Murphy, Shleifer, Vishny (1989)
- Dual economy:
  - Traditional (subsistence production): constant returns  $y_i = l_i$
  - Modern (industrial production):  $l_i = ay_i + F$  where  $a < 1$ ,  $F$  – fixed cost of modernization
  - Efficiency wage: employees of modern firms must be paid  $v$  per cent more.
- Also describes introduction of new technologies/standards
  - QWERTY vs DVORAK
  - VHS vs BETACAM
  - Mobile phone standards

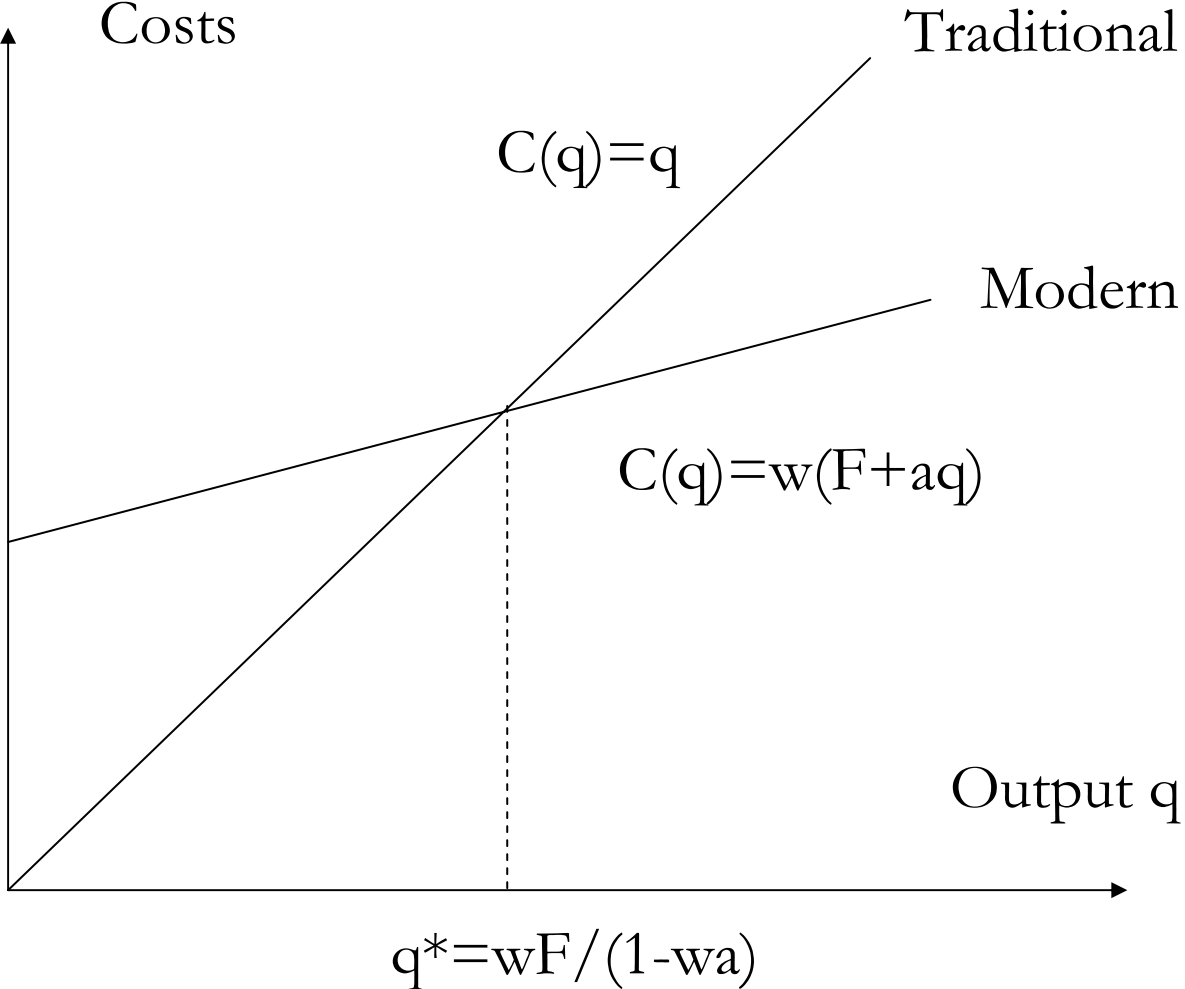
# Market size externality

- Entrepreneur  $i$  modernizes  $\Rightarrow$  workers at firm  $i$  his workers are better paid  $\Rightarrow$  aggregate demand increases
- Demand for all products increases, including product  $j$
- Makes easier for entrepreneur  $j$  to cover fixed costs
- Typical coordination game, multiple equilibria
  - Big Push, government intervention may be beneficial
- Another solution: increase market size through opening up and entering global market

# The choice of technology

- N sectors, in each entrepreneur compares
  - Traditional technology:  $l(q)=q$ ,
    - Productivity=wage=1
    - No fixed costs, but high marginal costs
  - Modern technology:  $l(q)=F+aq$ 
    - Large fixed costs  $F>0$ ,
    - Low marginal costs  $a<1$
    - Wage must be  $w>1$ ,  $wa<1$

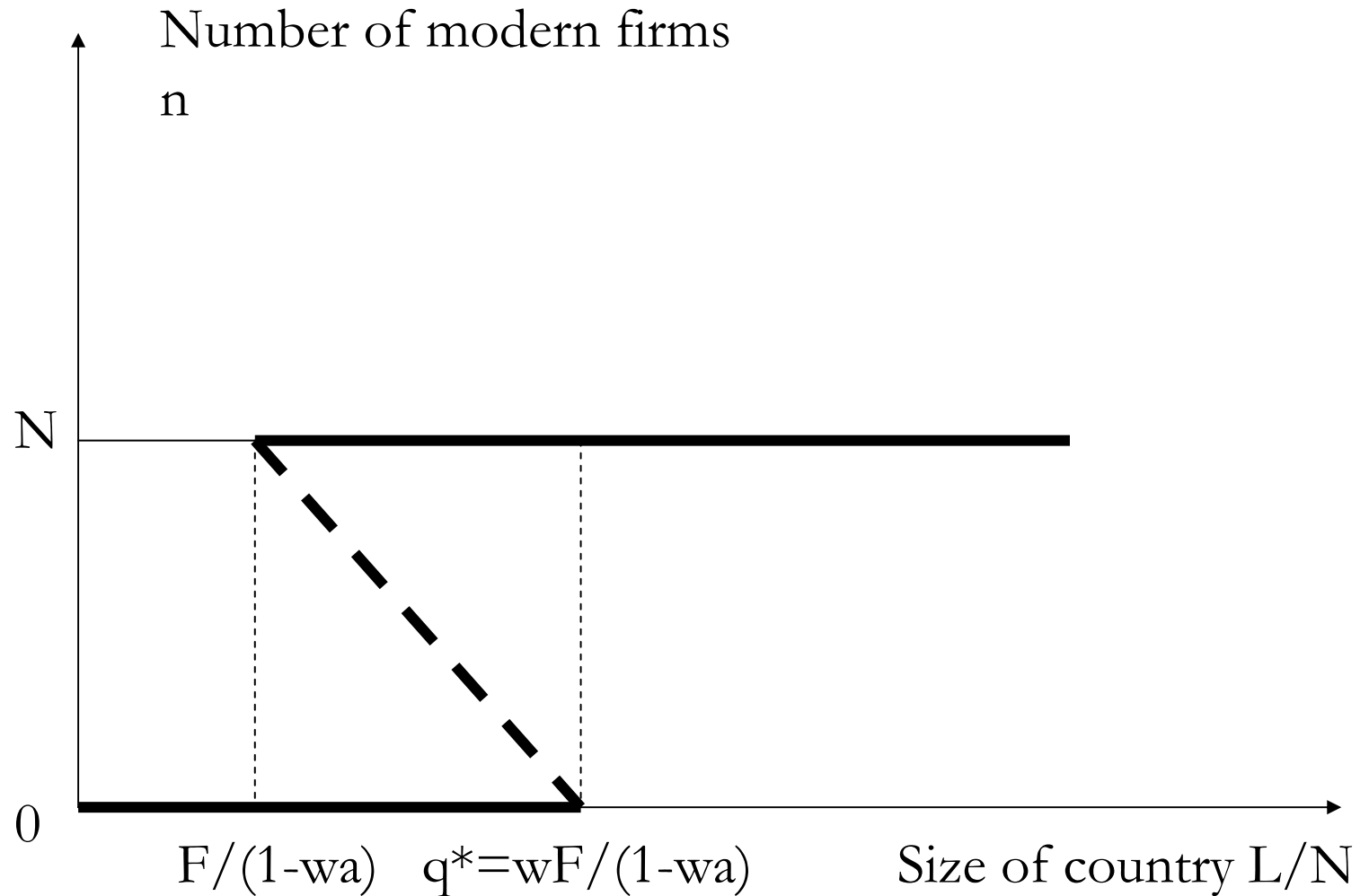
# Modern technology is better whenever demand is high



# Macroeconomic equilibrium

- GDP:  $Y=Nq$  hence each firm's demand in equilibrium is  $q=Y/N$
- Suppose that  $n$  firms choose modern technology
- Then labor market equilibrium:  
 $L=n(F+qa)+(N-n)q=n(F+aY/N)+(N-n)Y/N$   
 $q=(L-nF)/(N-n(1-a))$
- Compare  $q$  to  $q^*$ 
  - If  $q < q^*$ , all firms remain traditional  $n=0$   
 $L/N < q^* = wF/(1-wa)$
  - If  $q > q^*$ , all firms choose modern technology  $n=N$   
 $L/N > F/(1-wa)$
  - If  $q = q^*$ , some firms choose modern technology  $0 \leq n \leq N$ 
    - $F/(1-wa) < L/N < wF/(1-wa)$

# Structure of equilibria





# Recent literature on Schumpeterian growth

- Aghion et al.: “Distance to Frontier”
- The trade-off: imitate vs. innovate
  - Adopt technologies developed elsewhere vs
  - Develop new technologies
- If the country is far from frontier, imitation is optimal
  - Catching up growth: Korea and Japan until 1990s
  - Government intervention, larger vertical conglomerates etc.
- If the country is close to frontier, need to innovate
  - US, Western Europe
  - Decentralized, small firms, financial markets

# Empirical research on growth

- Large sample of countries: data available only for postwar period
- Hence only cross-section analysis is feasible
- Vulnerable to omitted variable bias and endogeneity
  - Good instrumental variables are hard to find

# Some cross-country datasets

- Summer Preston Penn World Tables  
Barro-Lee  
<http://www.economics.harvard.edu/faculty/barro/data.html>
- Barro-Sala-i-Martin  
[www.columbia.edu/~xs23/](http://www.columbia.edu/~xs23/)
- World Bank  
[www.worldbank.org](http://www.worldbank.org)
- Global Development Network  
[www.gdnet.org](http://www.gdnet.org)

# Meta-regressions

- Hundreds of cross-country regressions have been run producing different results
- Levine-Renelt AER 1992: extreme bounds test proves that no variables are robust
- Sala-i-Martin AER PP 1997 “I just ran 2 million regressions” uses a less extreme test
  - Select 62 variables
  - Add then in combination of fours with regression that already includes initial GDP per capita, life expectancy, primary school enrollment
  - Declare the variable “robust” if it is significant in 90% cases
  - Found 22 robust variables

# Sala-i-Martin's 22 variables

Independent variable	(i) $\beta$	(ii) SD			
Equipment investment	0.2175	0.0408	Fraction of GDP in mining	0.0353	0.0138
Number of years open economy	0.0195	0.0042	SD black-market premium	-0.0290	0.0118
Fraction Confucian	0.0676	0.0149	Primary exports in 1970	-0.0140	0.0053
Rule of law	0.0190	0.0049	Degree of capitalism	0.0018	0.0008
Fraction Muslim	0.0142	0.0035	War dummy	-0.0056	0.0023
Political rights	-0.0026	0.0009	Non-equipment investment	0.0562	0.0242
Latin America dummy	-0.0115	0.0029	Absolute latitude	0.0002	0.0001
Sub-Saharan Africa dummy	-0.0121	0.0032	Exchange-rate distortions	-0.0590	0.0302
Civil liberties	-0.0029	0.0010	Fraction Protestant	-0.0129	0.0053
Revolutions and coups	-0.0118	0.0045	Fraction Buddhist	0.0148	0.0076
			Fraction Catholic	-0.0089	0.0034
			Spanish colony	-0.0065	0.0032

# Summary of cross-country growth regressions

- Conditional convergence:
  - Other things equal, poor countries grow faster
- Quantity and especially quality of human capital increases growth
- Quality rather than size of government
  - Inflation, corruption, exchange rate regulation negatively affect growth
- Economic institutions are good for TFP growth ...
  - Property rights,
  - Rule of law
  - Financial development
- ... as well as the determinants of economic institutions
  - Economic geography and natural resource endowments
  - Colonial legacies, legal origin, religion
  - Ethnolinguistic fractionalization

# New Paradigm: Banerjee-Duflo / Rodrik

- Aggregate models miss the main issue (raised in Lucas, 1990):
  - The returns to investment in physical and human capital are different within poor countries
  - In aggregate models, there is no place for different rates of return
- The different rates of return are driven by poor institutions (property rights protection and contract enforcement), government predation, market failures, monopoly etc.
- Need disaggregated models that would describe this
  - And microeconomic evidence to test their predictions